

[ O19-109

[ > **restart:**

[ > **f:=(1-cos(x))/(x^(2/3));**

$$f := \frac{1 - \cos(x)}{x^{(2/3)}}$$

[ > **series(f,x=0);**

$$\frac{x^{(4/3)}}{2} - \frac{x^{(10/3)}}{24} + O(x^{(16/3)})$$

[ > **g:=diff(f,x);series(g,x=0);**

$$g := \frac{\sin(x)}{x^{(2/3)}} - \frac{2}{3} \frac{1 - \cos(x)}{x^{(5/3)}}$$
$$\frac{2 x^{(1/3)}}{3} - \frac{5 x^{(7/3)}}{36} + O(x^{(13/3)})$$

[ > **h:=diff(g,x);series(h,x=0);**

$$h := \frac{\cos(x)}{x^{(2/3)}} - \frac{4}{3} \frac{\sin(x)}{x^{(5/3)}} + \frac{10}{9} \frac{1 - \cos(x)}{x^{(8/3)}}$$
$$\frac{2}{9 x^{(2/3)}} - \frac{35 x^{(4/3)}}{108} + O(x^{(10/3)})$$

[ > **i:=int(f^2-g^2+h^2,x=1..t):evalf(subs(t=1.1,i));plot(i,t=1..2);**

$$-0.003581879969$$

